

### Challenge 2021 Maths III solutions

- 1) 55 minutes
- 2)  $x = -6, y = -2\frac{1}{2}$
- 3) 0.29kg
- 4) a) Angles in pentagon AFGCB =  $540^\circ$  so  $FGC = 130^\circ$   
b)  $FGE = 120^\circ$   
 $EGC = 110^\circ$   
 $EGC + GCD = 180^\circ$  hence result (co-interior angles)  
OR as  $FGE = 120^\circ$  then by alternate angles EG and FA parallel, which is parallel to DC.
- 5) 10:11 (two properties of wine in this question therefore 2D table ideal) (need to work with actual amount of wine, even though it's a ratio question, so red corked = x, for example)
- 6) 63, 98 (LCM question)
- 7) 16.5cm (3 scenarios. Water same in each. Form 2 equations (1<sup>st</sup> scenario and 2<sup>nd</sup> scenario gives relationship between  $r_1$  and  $r_2$  then solve using 1<sup>st</sup> scenario and 3<sup>rd</sup> scenario)
- 8) 16%
- 9) 12
- 10) 1 hour 24 minutes
- 11) a) 17  
b) 17 first and 4 second
- 12) HP win by 40 metres
- 13) a)  $x^2 - y^2$   
b) Annulus area =  $\pi \times 6.7^2 - \pi \times 3.4^2$   
 $= \pi(6.7^2 - 3.4^2)$   
 $= (6.7 + 3.3)(6.7 - 3.3)\pi$   
 $= 34\pi$   
c) 7.5cm, 9.5cm (as  $17 \times 2 = 34$ , so  $x+y=17$ ,  $x-y=2$ . Or use  $34 \times 1$  (though lots of other options))
- 14) a) 540  
b) 600