

Shrewsbury 2021 16+ entrance

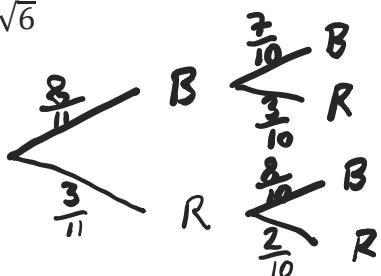
- 1) a) $27p + 2q$
 b) $48x^2 + 22xy - 15y^2$

- 2) a) $8h^3x^3(3h - 2x)$
 b) $(3p - 1)(p - 2)$

- 3) a) 64%
 b) £316.80
 c) £158

- 4) a) $5\frac{1}{10}$
 b) $5\sqrt{6}$

5) a)



b) $1 - \frac{8}{11} \times \frac{7}{10} = \frac{27}{55}$

- 6) a) 66

- b) 45

- 7) a) 12.5cm

- b) 32.6°

- 8) a) 2

- b) 3.3

- c) 5

9) a) $C = \frac{R-5}{3}$

b) $C = \frac{3}{U} + 1\frac{1}{2}$

10) $\frac{2(x-2)}{x+1}$

B1) 1

Please turn over

B2)a) $4! = 24$

b) $\frac{4!}{4} = 3! = 6$

c) Options for layout (x, x same author, A, B, C, D other books):

x	x		
x		x	
x			x
	x	x	
	x		x
x			x
	x	x	
	x		x
		x	x

9 options

x and x can be interchanged so multiply by 2

A, B, C, D can be interchanged so multiply by 4!

divide by 6 due to rotation:

$$\frac{(9 \times 2 \times 4!)}{6} = 72 \text{ options}$$

Or: $\frac{6!}{6}$ ways of arranging 6 books in a circle. If two are by the same author then

consider 5 units (one of which is two books), which can be arranged in $\frac{5!}{5} = 24$ ways. Double because the two books can be two ways around: 48. $120-48=72$.

B3)a) $x^2 - 2 + \frac{1}{x^2}$

b) $u^2 + 2$

c)

$$\begin{aligned} x^2 - x - 4 + \frac{1}{x} + \frac{1}{x^2} \\ = x^2 + \frac{1}{x^2} - \left(x - \frac{1}{x}\right) - 4 \\ = u^2 + 2 - u - 4 \\ = u^2 - u - 2 \\ = (u - 2)(u + 1) \end{aligned}$$

So $u = 2$ or $u = -1$

$$x - \frac{1}{x} = 2 \text{ gives } x^2 - 2x - 1 = 0 \text{ so } x = 1 + \sqrt{2} \text{ or } x = 1 - \sqrt{2}$$

$$x - \frac{1}{x} = -1 \text{ gives } x^2 + x - 1 = 0 \text{ so } x = \frac{-(1+\sqrt{5})}{2} \text{ or } x = \frac{-(1-\sqrt{5})}{2}$$

d) Same as part c) except that $y^2 = x$.

$$\text{So } y^2 = 1 + \sqrt{2} \text{ or } y^2 = \frac{-1+\sqrt{5}}{2} \text{ (need positive values)}$$

$$\text{So } y = \pm\sqrt{1 + \sqrt{2}} \text{ or } y = \pm\sqrt{\frac{-1+\sqrt{5}}{2}}$$